# 4748-120 (Evolve) and 4748-220 (Paper-based) <br> Functional Skills Mathematics Level 2 <br> <br> Guidance for Delivery 

 <br> <br> Guidance for Delivery}

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## 1. Introduction

The following document is intended to support tutors with the delivery of the reformed Level 2 Functional Skills mathematics qualifications.

This should be read in conjunction with the following

- DfE Subject content functional skills: Mathematics

The new subject content requires candidates to demonstrate their competence (functionality) in mathematics at the appropriate level. Achievement of the qualification demonstrates a sound grasp of mathematical skills at the appropriate level, and the ability to apply mathematical thinking effectively to solve problems successfully in the workplace and in other real life situations.

Although there is an emphasis on work-based contexts and financial literacy, the assessments are generic rather than vocationally based.

The subject content is split into three areas: using numbers and the number system; using common measures, shape and space; and handling information and data / statistics. There is naturally much overlap between these sections and drawing on different areas should be encouraged when preparing learners for assessment.

## 2. Structure of the assessment

Level 2 Functional Mathematics papers comprise two sections: a short section without a calculator available and a longer section in which a calculator is permitted. Within both sections there are context-free questions testing underpinning skills and knowledge and there are problem solving questions requiring candidates to tackle problems in more complex contexts, ie, problems requiring a multistep process requiring some planning and working through at least two connected steps. Candidates will be required to analyse the problems to decide suitable approaches, tackle the problems, achieve solutions and explain findings. Problem-solving questions will account for $75 \%$ of the marks on each paper.

|  | Part 1 <br> Calculator not permitted (25 minutes) | Part 2 <br> Calculator permitted <br> (1 hour 20 minutes) |
| :---: | :---: | :---: |
| Underpinning knowledge (15 marks = 25\%) | 10 single mark context free questions | 5 single mark context free questions |
| Problem solving <br> (45 marks = 75\%) | Between 2 to 5 problem solving questions with practical context (total 5 marks) | 1 single mark check (for sense of result) <br> 9 problem solving questions with practical context <br> (mark tariff between 2 and 6 marks each, total 39 marks) |

There are two options for assessment:

- an onscreen test (E-volve)
- a paper-based test

Both options are available on demand.

## 3. Duration

The Level 2 assessment is 1 hour and 45 minutes.
Section 1 is 25 minutes.
Section 2 is 1 hour and 20 minutes.

## 4. General

The assessment is based on this specification, and teaching should reflect the subject content.

Regardless of which assessment option is chosen, candidates should be familiar with sample papers, which are indicative of content. Both onscreen ( E -volve) and paper-based samples will assist this process. Samples of both types are available on the City and Guilds website (found here). It is also important that candidates are aware of the format of the option they have chosen. E-volve candidates should be given the opportunity to practise onscreen samples. They should be aware that answers must be recorded in the answer boxes where provided and working should be shown in the spaces provided for working. Candidates who fail to do these things will be unable to access compensation marks if their final answer is incorrect. Candidates should be encouraged to practise using the tools in the E-volve test by accessing the familiarisation tool found here. Practise with options 1 (calculator and work box), 5 (table), 7 (diagram), 8-11 (charts and graphs) will be of particular value to Level 2 candidates.

In the E-volve test, for the second section only, candidates will have access to a basic onscreen calculator. However candidates are permitted to use their own (more sophisticated) calculators and should be advised to do so.

Candidates opting for paper-based assessment should likewise be given the opportunity to practise sample papers. They must also answer in the spaces provided and are advised to show working in order to secure compensation marks if their final answer is incorrect. They must have rulers in order to successfully attempt some of the questions and calculators for the calculator permitted section.

## 5. Underpinning skills and problem solving

Each of the two Sections will contain a balance of problem solving and underpinning skills questions.

Overall $25 \%$ of the marks will be for UPK and $75 \%$ for problem solving.

- Section 1 has 10 marks for underpinning skills followed by 5 marks for problem-solving.
- Section 2 starts with 5 marks for underpinning skills and the remaining 40 marks are for open response problem solving questions.


## Underpinning skills questions

The first 10 marks in Section 1 and the first 5 marks in Section 2 are for underpinning skills. These questions will normally have no context or a very limited context and minimal reading demand. They are designed to assess standard mathematical processes for the level.

## Problem-solving questions

The final 5 marks in Section 1 and the final 40 marks of Section 2 assess problem solving.
Each question will be a single realistic problem based on a topic that (some) people might reasonably meet in everyday life or work. However, as the assessment is not vocationally specific, problems will be generic in nature and therefore not necessarily related to immediate experiences of all candidates.

Ofqual define a problem as

- having little or no scaffolding: there is little guidance given to the student beyond a start point and a finish point. Questions do not explicitly state the mathematical process(es) required for the solution.
- information not given in mathematical form or in mathematical language; or there is a need for the results to be interpreted or methods evaluated, for example, in a real-world context.

Therefore, problem-solving questions will generally not have specific instructions that give the method such as

- Work out the total cost.
- Draw a line of symmetry on the outline.

Instead candidates are more likely to come across questions, eg

- Is the manager correct?

Explain your answer.

- Which type of ticket do you recommend?

Explain your reasons. Include figures or calculations to support your decision.

- Did the changes make any difference?

Explain your findings to the manager. Show calculations to support your explanation.

- Will the man be better off in the new job?

Give a reason for your answer.

Candidates will be expected to choose an appropriate approach and methods as well as carry out calculations. They will also be given opportunities to interpret information.

## 6. Question types

Papers will be a mixture of the following question types, whichever format the learner opts to sit:

- short answer
- multiple choice question (MCQ)
- producing a graph / chart / table / diagram.

Drawing graph/chart items Each paper will have one question that requires the candidate to construct a chart or graph OR diagram (see below). They will have to choose titles and axis labels; choose a suitable scale and plot bars or lines.

Drawing diagram items A paper may require the candidate to draw a diagram instead of a graph or chart.

It is strongly recommended that candidates taking the E-volve papers practise drawing charts, graphs and diagrams with the online tools in advance of sitting the paper.

## 7. Sample papers

Sample assessments can be found on the City \& Guilds website at the following link: www.cityandguilds.com/what-we-offer/centres/maths-and-english/functional-skills

## 8. Tips

### 8.1. Subject content

Centres should be aware of all the detailed subject content specified for Level 2 in the DfE Subject content document (DfE Subject content functional skills: Mathematics) and be aware that Level 2 content also subsumes all level content below Level 2.(see appendix 2)

Particular attention is drawn to the following significant 'upgrading' from previous Level 2 specifications (numbers refer to DfE Subject content):
19. Use coordinates in 2-D, positive and negative, to specify the positions of points
21. Draw 3-D shapes to include plans and elevations
22. Calculate values of angles and/or coordinates with 2-D and 3-D shapes
24. Estimate the mean of a grouped frequency distribution from discrete data
26. Work out the probability of combined events including the use of diagrams and tables including two-way tables
28.Draw and interpret scatter diagrams and recognise positive and negative correlation

### 8.2. General calculation issues

Candidates must understand order of operations conventions (BIDMAS) and apply them to calculations. Online Candidates should be aware that the E-volve calculator currently does not automatically apply BIDMAS.
Candidates must also be able to apply these rules when using formulae, including algebraic equations.
Candidates should use estimation and approximation techniques when required, including checking calculations.

### 8.3. Explanations / comments needed for problem solving questions

Problem solving questions may specify a requirement for explanation (comments). Candidates must be aware that, although marks will be awarded for relevant calculations, full marks will require a suitable explanation using their results, preferably with reference to numerical values calculated: eg the first option is cheaper by $£ 4.50$
eg, $A$ is warmer than $B$ average temperature for $A$ is $26^{\circ} \mathrm{C}>19^{\circ} \mathrm{C}$ for $B$

Candidates must also be prepared to explain why an answer is sensible (or not) based on mathematical process rather than calculated results.

Candidates should be taught the distinction between averages and range and how to use each in explanations in context.

### 8.4. Presentation of results / workings

The importance of showing working on the assessments, ie to show calculations and methods used, should be stressed, particularly so that potential compensation marks, in the event of incorrect answers, are accessible to the candidate. This should be emphasised to online candidates who may use 'pencil and paper' methods initially to formulate their solutions.

Candidates need to understand the use of scales in scale diagrams and be prepared to construct scale diagrams, including plans and elevations.

Candidates should be taught to use a variety of presentation methods to summarise results, including graphs, charts and tables. They must understand that a table is not a chart (and vice versa). Summary tables should be systematically constructed to include rows and columns with appropriate headings.

Level 2 candidates must be prepared to construct scatter graphs and to draw and understand trend lines.

Additionally, they may require presentation methods listed in the Level 2 subject content (27), ie line graphs, bar charts and pie charts.

Candidates who choose to access assessment online need to be prepared not only in terms of the prescribed Functional Skills Specification, but also in terms of using the Evolve platform. They must be well practiced in the use of the presentation tools (tables, diagrams, charts and graphs) including how to insert sufficient text, keys and the use of sensible scales.

## Appendix 1 Amplification of (DfE Subject Content)

Functional Skills mathematics qualifications at Level 2 should:
> Indicate that students can demonstrate their ability in mathematical skills and their ability to apply these, through appropriate reasoning and decision making, to solve realistic problems of increasing complexity;
> Introduce students to new areas of life and work so that they are exposed to concepts and problems which, while not of immediate concern, may be of value in later life; and
> Enable students to develop an appreciation of the role played by mathematics in the world of work and in life generally

### 1.1 Overview of Level 2 Functional Maths requirements

Centres should use the broad outline presented below in conjunction with the subject criteria specifications (SCS).

[^0]calculate and interpret probabilities. They can calculate, analyse, compare and interpret appropriate data sets, tables, diagrams and statistical measures such as common averages (mean, median, mode) and spread (range), and use statistics to compare sets of data. They can identify patterns and trends from data as well as recognise simple correlation.

### 1.2 Subject Content Specifications (SCS)

## 1. Read, write, order and compare positive and negative numbers of any size

> large and small numbers written as numbers, words or powers of 10
million $(\mathrm{m})=10^{6}=1000000$
billion $(b n)=10^{9}=1000000000$ (one thousand million as used in finance eg \$4bn)
> Write amounts of money correct to two dp in the correct context
Eg: The total amount of money on an order form would be $£ 134.70$, NOT $£ 134.7$
$>$ put the following in increasing order:
3050 three hundred and sixty two $3 \times 10^{3} \quad-351 \quad 0 \quad-3$
2. Carry out calculations with numbers up to one million including strategies to check answers including estimation and approximation.
> add, subtract, multiply, divide, use indices
$10^{3} \times 10^{2}=10^{5}(=100000) \quad 10^{3}+10^{2}=1100$
$>\frac{1}{3} \times 21$ is $21 \div 3$
$>$ round numbers to the nearest $1,10,100,1000$
15 to nearest $10=20,2.6$ to the nearest $1=3$
$>$ round numbers to given number of decimal places 65.3794 to $2 d p$ is 3 dp
> round numbers to given numbers of significant figures 65.3794 to 3 sig figures is 65.4
$>$ understand when rounding up and rounding down is appropriate eg round up 14.6 to 15 (rolls of wall paper as cannot buy 0.6 rolls)
eg round down (truncation) 6.7 to 6 (number of applications of fertiliser as 0.7 is not enough for a complete application)
$>$ check by approximation eg $25 \times 50=1250$ checks $24 \times 48=1152$
$>$ check by reverse calculation eg $1152 \div 48=24$ checks $24 \times 48=1152$
3. Evaluate expressions and make substitution in given formulae in words and symbols.
> simple algebraic equations
$\begin{array}{ll}a+2 b^{2}=36 \text { what is } b \text { if } a=4 & (b=4) \\ 3 x y=12\end{array}$
$3 x y=12$ what is $y$ if $x=4 \quad(y=1)$
> know the difference: xy (represents x multiplied by y ) is not same as $\mathrm{x}+\mathrm{y}$ ( x added to y ) and similarly 2 y is 2 multiplied by y and $\frac{y}{2}$ is the same as $\frac{1}{2} y$ ( y divided by 2 )
> substitute values into formulae in symbols
eg $V=\frac{\pi r^{2} h}{3} \quad$ for volume of cone

> substitute values into word formulae
eg monthly payment $=\frac{\text { total cost }+13.5 \%}{\text { period of loan in months }}$ for repayment of bank loan
4. Identify and know the equivalence between fractions, decimals and percentages.
$>$ equivalence $\frac{1}{10}=10 \%=0.1=10^{-1} \quad \frac{1}{100}=1 \%=0.01=10^{-2}$
$>$ percentages as decimals $5 \%=0.0550 \%=0.5$
$>$ fractions as decimals eg $\frac{3}{16}=3 \div 16$ (on calculator) $=0.1875$
$>$ convert harder fractions with calculator, eg one millionth $\frac{1}{1000000}=0.000001$
$>$ decimals rounded to given number decimal places (dp) eg 0.1875 to $2 d p=0.19$
$>$ fractions expressed in simplest form $\frac{44}{121}=\frac{4}{11}$
$\Rightarrow$ put the following in decreasing order $\frac{1}{30} \quad 0.3 \quad \frac{1}{300} \quad 33 \%$

## 5. Work out the percentages of amounts and express one amount as a percentage of another

> percentages of amounts
$6 \%$ of $250=15$ from $0.06 \times 250$ (calculator) or $250 \div 100 \times 6$ (non calculator)
$>$ amount as a percentage of another
18 as a percentage of $120=15 \%$
6. Calculate percentage change (any size increase and decrease) and original value after percentage change
> percentage increase
200 increased by $40 \%=280$ from 200x 1.4 (derived from $1+0.4$ )
> percentage decrease
200 decreased by $40 \%=120$ from $200 \times 0.6$ (derived from $1-0.4$ )
$>$ percentage change
$£ 720$ find price before VAT added $=£ 600$
Including 20\% VAT from $\frac{720}{120} \times 100=600$

| Company results |  |  |
| :---: | :---: | :---: |
| find the percentage increase in profit $=25 \%$ |  |  |
| year | 2019 | 2020 |
| from $\frac{10000-8000}{8000} \times 100=25$ |  |  |
| profit | $£ 8000$ | $£ 10000$ |
|  |  |  |

7. Order, add, subtract and compare amounts or quantities using proper and improper fractions and mixed numbers
$>$ proper fractions: greater than 0 but less than 1 , eg $\frac{3}{4}$
> improper fractions: greater than 1, eg $\frac{4}{3}$
> mixed numbers, eg $\frac{4}{3}$ (improper fraction) $=1 \frac{1}{3}$
place the following in order of decreasing value: $\frac{1}{2}, \frac{7}{3}, \frac{1}{23}, \frac{9}{2}, 1 \frac{1}{5}$
ie $\frac{9}{2}, \frac{7}{3}, 1 \frac{1}{5}, \frac{1}{2}, \frac{1}{23}$
$>$ present fractions in simplest form (division of numerator and denominator by common divisor) eg $\frac{28}{35}=\frac{4}{7}$
> addition and subtraction of fractions using common denominator

$$
\begin{aligned}
& 3 \frac{1}{7}+\frac{23}{35}=\frac{22}{7}+\frac{23}{35}=\frac{110+23}{35}=\frac{133}{35} \\
& =3 \frac{28}{35}=3 \frac{4}{5} \\
& 3 \frac{1}{7}-\frac{12}{35}=\frac{22}{7}-\frac{12}{35}=\frac{110-12}{35}=\frac{98}{35} \\
& =2 \frac{28}{35} \quad=2 \frac{4}{5}
\end{aligned}
$$

> Note: multiplication and division using fractions is also required (when using formulae) using cancellation

$$
\begin{gathered}
V=\pi r^{2} h \\
V=\frac{22}{7} \times 49 \times 10 \\
V=\frac{22}{7} \times 497 \times 10 \\
V=1540
\end{gathered}
$$

## 8. Express one number as a fraction of another

$>$ evaluate the size of one number compared to another, eg 2 is $\frac{1}{10}$ of 20 .
$>$ present answer in simplest form (see also SCS 7), eg $\frac{3}{27}=\frac{1}{9}$
what fraction of 250 is $50 ? \quad \frac{50}{250}=\frac{1}{5}$

## 9. Order, approximate and compare decimals

> understand significance of decimal point position
0.1 is ten times larger than 0.01
0.003 is one thousand times smaller than 3
> approximate values to given numbers of decimal places (dp)
3.94352 to $2 d p$ is 3.94
3.94352 to 3 dp is 3.944
> approximate decimal values to percentage and fraction equivalents (see also SCS4)
$0.97 \approx 100 \% \quad 0.7666 \approx 77 \%$
$0.247 \approx \frac{1}{4}$
> know when it is inappropriate to use approximate values in calculations
eg one third of $£ 57$ is $\frac{1}{3} \times £ 57=£ 19$ NOT $0.33 \times £ 57=£ 18.81$
> order decimals
place the following in increasing order of value:
7.6511 .7651 .0761 .5671 .657 (ie 1.0761 .5671 .6571 .7657 .651 )

## 10. Add, subtract, multiply and divide decimals up to 3 decimal places

> without calculator
eg $0.65+0.345$

| 0.65 | 0.735 |
| :---: | :---: |
| +0.345 |  |
| $\mathbf{0 . 9 9 5}$ |  |

eg $2.25 \times 0.02=0.045$
eg $4.50 \div 0.05=90$
$>$ with calculator
care required when reading decimal points, encourage checking for sense
eg $34.12 \times 12.541 \neq 4278.989$ (approximation $30 \times 10=300$ means result of wrong order of magnitude)
11. Understand and calculate using ratios, direct proportion and inverse proportion.
> use a ratio to calculate amounts; ratio expressed as $4: 7$ is based on 11 parts
eg 140 kg concrete made from 1 part cement : 2 parts sand : 4 parts gravel sand required $=(140 \div 7) \times 2=40 \mathrm{~kg}$
$>$ simplify a ratio, e.g 4:8 is the same as 1:2
$>$ direct proportion - as one number increases, the other increases proportionally $(y=k x)$. eg a 250 g pack of butter contains 897.5 calories, how many calories in 100 g ?
$(900 \div 250) \times 100=360$ calories
(ie $\mathrm{y}=\mathrm{kx} ; 900=250 \mathrm{k} ; k=\frac{900}{250}=3.6 ; y=100 \times 3.6=360$ )
$>$ inverse proportion- as one number increases, the other decreases proportionally ( $y=k / x$ ) eg a journey takes 4 hours at an average speed of 50 mph , how much longer will the journey take at an average speed of 40 mph ?
$\frac{5}{4} \times 4=5$ hours
(ie $y=\frac{k}{x} ; 50=\frac{k}{4} ; k=4 x 50=200 ; x=\frac{200}{40}=5$ )
$>$ understand slope (gradient) expressed as eg 1 in 10 or 10\%


1 m
Gradient 1 in 10 or $10 \%$

Gradient
1 in 4 or $25 \%$ is steeper than
> Understand converting amounts of money from one country to another given a conversion rate

Eg: $\$ 1$ (USD) $=€ 0.94$ Euro. What is the value of $€ 230$
$230 \div 0.94=\$ 244.68$

## 12.Follow the order of precedence of operators including indices

> Calculate numbers with indices

$$
3^{2}=3 \times 3=9 \quad 3^{3}=3 \times 3 \times 3=27 \quad 3^{4}=3 \times 3 \times 3 \times 3=81
$$

$>$ Calculate whole number square roots

$$
\sqrt{25}=5
$$

> understand and use BIDMAS (order of operations) when making calculations

| B | brackets |
| :--- | :--- |
| I | indices |
| D | division |
| M | multiplication |
| A | addition |
| S | subtraction |

eg $3^{4}+7 \times 3-9=98$

| first | $3^{4}$ | 81 |
| :---: | :---: | :---: |
| second | $7 \times 3$ | 21 |
| third | $81+21$ | 102 |
| fourth | $102-4$ | 98 |

$$
\left(3^{4}+7\right) \times(3-9)=-528
$$

$$
\left(3^{4}+7\right) \times 3-9=253
$$

| first | $3^{4}+7$ | $81+7$ <br> $=88$ |
| :---: | :---: | :---: |
|  | $3-9$ | -6 |
| second | $88 x-6$ | -528 |


| first | $3^{4}+7$ | $81+$ <br> $7=$ <br> 88 |
| :---: | :---: | :---: |
| second | $88 \times 3$ | 264 |
| third | $264-9$ | 253 |

particularly important in some given formulae
eg $\quad A=\frac{\pi\left(D^{2}-d^{2}\right)}{4}$ for outer area

## 13.Calculate amounts of money, compound interest, percentage increases, decreases and discounts including tax and simple budgeting

> calculate a percentage increase
eg add $20 \%$ VAT to a bill for $£ 27.65$
$27.56 \times 1.2=£ 33.18$
> calculate a percentage decrease
eg what money is left after income tax for a person earning $£ 35000$ per year
personal allowance (given) is $£ 12500$, taxable pay $=£ 35000-12500=£ 22500$
money left $=12500+22500 \times 0.8=£ \mathbf{5 0 5 0 0}$
$>$ calculate a percentage change using $\frac{\text { new value-old value }}{\text { old value }} \times 100 \%$
eg a company makes a profit of $£ 160000$ in 2019. In 2020 the profit is $£ 180000$. What is the percentage increase in profit?

$$
\frac{180000-160000}{160000} \times 100=12.5 \%
$$

understand simple interest as a one-off addition of a percentage to an original amount eg a man puts $£ 1000$ in a savings account that pays interest at $1.5 \%$ per year - what is the amount he has after one year?
amount after one year $=$ original amount $+1.5 \%$ of original amount $=1000+15=£ 1015$
understand compound interest as accumulated interest paid on a number of regular occasions (interest is added to each new amount)
eg a man puts $£ 1000$ in a savings account that pays interest at $1.5 \%$ per year for 3 years - what is the amount he has after the three years: $£ 1045.68$

|  | amount at <br> start of year <br> (£) | + | interest (£) | amount (£) |
| :--- | :--- | :--- | :--- | :--- |
| year 1 | 1000 | + | $1000 \times 0.15$ | 1015 |
| year 2 | 1015 | + | $1015 \times 0.15$ | 1030.225 |
| year 3 | 1030.225 | + | $1030.225 \times 0.15$ | $\mathbf{1 0 4 5 . 6 7 8 3 7 5}$ |

understand and use a given formula for compound interest calculations:
eg $A=P(1+r)^{t}$
where $A$ is amount at end of period
$P$ is amount at start of period
$r$ is the \% interest expressed as decimal fraction
$t$ is the number of times interest is applied
for the example above:

$$
\begin{aligned}
& A=1000(1+0.15)^{3} \\
& A=1000 x(1.015)^{3} \\
& A=£ 1045.68
\end{aligned}
$$

understand and calculate simple accounting / budgeting
eg complete the profit and loss table (answer in red)

| February profit / loss |  | running total |  |
| :--- | ---: | ---: | ---: |
| week 1 | $-£ 121.60$ |  | $-£ 121.60$ |
| week 2 | $£ 213.40$ | $£$ | 91.80 |
| week 3 | $-£ 35.60$ | $£$ | 177.80 |
| week 4 | $£ 106.50$ | $£$ | 70.90 |
|  | total | $£$ | 162.70 |

eg make a customer bill

| PAINT SHOP CUSTOMER BILL |  |  |  |
| :---: | :---: | :---: | :---: |
|  |  | unit price | cost (£) |
| paint | 3 tins | 19.99 | 59.97 |
| brushes | 2 | 3.99 | 7.98 |
| sub total |  |  | 67.95 |
| 12.5\% customer discount |  |  | -8.49 |
| total |  |  | 59.46 |
| VAT @ 20\% |  |  | 11.89 |
| total to pay |  |  | 71.35 |

## 14. Convert between metric and imperial units of length, weight and capacity using a) a conversion factor and b) a conversion graph

> convert within same system
1 metre $=100 \mathrm{~cm}=1000 \mathrm{~mm}$
NB do not confuse linear measure with area and volume measures
eg $1 \mathrm{~m}^{2}=10000 \mathrm{~cm}^{2}$ not $1000 \mathrm{~cm}^{2}$
$10000 \mathrm{~m}^{2}=1$ hectare
1 tonne $=100 \mathrm{~kg} \quad 1 \mathrm{~kg}=1000 \mathrm{~g} \quad 1 \mathrm{~g}=1000 \mathrm{mg}$
1 litre $=1000 \mathrm{ml}$
> know common imperial measures
12 inches $=1$ foot 3 feet $=1$ yard
1 pound = 16 ounces
8 pints $=1$ gallon
> convert across systems with given conversion factors
miles to km;
yards or feet to m or cm
pounds to kg
also ${ }^{\circ} \mathrm{F}$ to ${ }^{\circ} \mathrm{C}$
eg kilometres to miles 1 mile $=1.6093 \mathrm{~km}$
what is 130 km in miles?
$130 \div 1.6093=80.78$ miles (to 2 dp ) check for sense: $1<1.6$, so miles will be fewer than km
eg Is 50 kph the same as 30 mph ?
$50 \div 1.6093=31.07 \mathrm{mph}$ or $30 \times 1.6093=48.28 \mathrm{kph}$ No, 50 kph is more than 30 mph
Understand that conversions between measures may require different level of accuracy
Eg: $10 z=25$ g or $10 z=28.2495$ grams depending on context.
> use conversion graphs
eg what is 65lbs in kg ?


## 15. Calculate using compound measures including speed, density and rates of pay

understand compound measures expressed as eg miles per hour that per indicates division
calculate speed, distance and time making sure that units are consistent


$$
\begin{aligned}
& \text { speed }(S)=\operatorname{distance}(D) \div \text { time }(T) \\
& \text { distance }(D)=\text { speed }(S) x \text { time }(T) \\
& \text { time }(T)=\operatorname{distance}(D) \div \text { speed }(S)
\end{aligned}
$$

eg how long will it take someone to walk 7.5 km at 4 kph pace?
$\mathrm{T}=\mathrm{D} / \mathrm{S}$, so $\mathrm{T}=7.5 \div 4=1.875$ hours
$0.875 \times 60=52.5$ minutes
Answer: 1hour 52.5minutes
> calculate and use density expressed as mass / volume eg $19.32 \mathrm{~g} / \mathrm{cm}^{3}$ for gold


$$
\begin{aligned}
& \text { density }(\mathrm{d})=\text { mass }(\mathrm{m}) \div \text { volume }(\mathrm{v}) \\
& \text { mass }(\mathrm{m})=\text { density }(\mathrm{d}) \times \text { volume }(\mathrm{v}) \\
& \text { volume }(\mathrm{v})=\text { mass }(\mathrm{m}) \div \operatorname{density}(\mathrm{S})
\end{aligned}
$$

eg A wood beam measures $20 \mathrm{~m} \times 50 \mathrm{~mm} \times 400 \mathrm{~mm}$ and has a density of $500 \mathrm{~kg} / \mathrm{m}^{3}$.
What is the weight (mass) of this beam?
Make sure units are consistent: $20 \times 0.05 \times 0.4=0.4 \mathrm{~m}^{3}$
$\mathrm{m}=\mathrm{dxv} \mathrm{m}=500 \times 0.4=200 \mathrm{~kg}$
> calculate and use rates of pay
eg a 19 year-old worker, on the national minimum wage, works $371 / 2$ hours a week. How much will the worker earn per year?

| National minimum wage |  |  |  |  |
| ---: | :---: | :---: | :---: | :---: |
| age | Apprentice | $16-17$ years | $18-20$ years | $21-24$ years |
| rate per hour | $£ 3.90$ | $£ 4.35$ | $£ 6.15$ | $£ 7.70$ |

$6.15 \times 37.5 \times 52=£ 11992.50$
16. Calculate perimeters and areas of 2-D shapes including triangles and circles and composite shapes including non-rectangular shapes (formulae given except for triangles and circles)
> know basic properties of all triangles: three sides, degrees add up to 180
> must know perimeter = lengths of all 3 sides added together
> must know area $=1 / 2$ base x vertical height


3 sides equal length
Each angle $=60^{\circ}$

b
$>$ know basic properties of circles: circumference; diameter $=2 \mathrm{x}$ radius
$>$ must know circumference (perimeter) $C=\pi d$ or $C=2 \pi r$
> must know area $A=\pi r^{2}$
$>$ if value for $\pi$ given eg 3.14 or $\frac{22}{7}$, then candidates must use the given value
$>$ if value for $\pi$ not given, candidates may use pi button on calculator or any other suitable value eg 3.142, 3.14 or $\frac{22}{7}$

$>$ know basic properties of regular quadrilaterals: 4 sides; parallels; diagonals, angles add up to $360^{\circ}$
> must know perimeter = lengths of all 4 sides added together
> must know area for rectangle/square $=$ length x breadth
> calculate other areas for quadrilaterals from composite areas of triangles

eg What is perimeter of this regular quadrilateral?

perimeter $=70+20+20+70=180 \mathrm{~m}$
$>$ calculate areas and perimeters of composite shapes
eg A carpenter cuts a semicircle from a regular trapezoid wood piece.
What is the area of the remaining wood?
Use $\pi=\frac{22}{7}$


$$
\begin{aligned}
& \text { Area of trapezium }=2 \Delta+\square \\
& =(2 \times 1 / 2 \times 15 \times 40)+(40 \times 40) \\
& =600+1600=2200 \mathrm{~cm}^{2} \\
& \text { Area of semi circle (radius }=14) \\
& =1 / 2 \times \frac{22}{7} \times 14 \times 14=308 \mathrm{~cm}^{2}
\end{aligned}
$$

Answer 2200-308 = 1892cm ${ }^{2}$
eg A painter needs to know the area of a wall.


What is the area of the wall?
Rectangle $=8 \times 4=32$
Triangle $=1 / 2 \times 8 \times 3=12$

$$
32+12=44 \mathrm{~m}^{2} \text { Answer }
$$

17. Use formulae to find volumes and surface areas of 3-D shapes including cylinders (formulae to be given for 3-D shapes other than cylinders)

## Note: formulae requiring calculation of square roots will not be used

> know how to substitute into and calculate with given formulae formulae will be given for 3-D shapes except cuboids and cylinders
$>$ value for pi $(\pi)$ often given in question and should be used. If value not given, candidates may use any from $\pi=\frac{22}{7} \pi=3.14 \quad \pi=3.142$ or $\pi$ value from calculator
$>$ be aware of common error : if diameter labelled, it must be halved if radius required in formula
eg sphere
$V=\frac{4 \pi r^{2}}{3} \quad$ or $\quad V=\frac{4}{3} \pi r^{2} \quad$ for volume

$A=4 \pi r^{2} \quad$ for surface area
eg tetrahedron (4-sided pyramid)
$V=\frac{L B H}{3} \quad$ or $\quad V=\frac{1}{3} L B H$ for volume
$A=L B+(L+B) S$ for surface area

eg cone (volume only)
$V=\frac{\pi r^{2} h}{3} \quad$ for volume of cone

> must know formulae for cylinder
$V=\pi r^{2} h$
$A=2 \pi r^{2}+2 \pi r h$


## 18. Calculate actual dimensions from scale drawings and create a scale diagram given actual measurements

> understand and use scales given
eg 1:10 means 1 unit represents 10 units
eg 1:25000 means 1 unit represents 25000 units
Although Level 2 candidates are expected to understand scales expressed in the above form, simpler explanations are also acceptable.
eg the scale is 2 squares $=1$ metre, so 3 metres is 6 squares
eg 1 cm represents 50 cm and 6 cm is $300 \mathrm{~cm}=3 \mathrm{~m}$
$>$ understand the principle of scaling up (reading actual measurements from a scale plan) eg 15 cm on a scale plan drawn 1:200 is ( $15 \mathbf{X} 200$ ) $\mathrm{cm}=3000 \mathrm{~cm}=30 \mathrm{~m}$
eg 5 cm on a map with scale $1: 25000$ is $(5 \mathbf{X} 25000) \mathrm{cm}=125000 \mathrm{~cm}=1.25 \mathrm{~km}$
$>$ understand the principle of scaling down (converting actual measurements for drawing a scale plan)
eg draw a floor area 12 m by 8 m to scale 1:50
$12 \mathrm{~m}=1200 \mathrm{~cm} 1200 \div 50=24 \mathrm{~cm}$ on plan; similarly $800 \div 50=16 \mathrm{~cm}$ on plan
> Graph paper used in assessments will normally be 2 mm graph paper. In the online environment, clearly the graph paper will not be actual size, but candidates may assume that each small square measures 2 mm .
read a scale plan
eg A farmer need to put fencing around a field and buy a gate. He has the following scale plan of the field.

How many metres of fencing does he need and what width gate must he buy?

Plan: fence perimeter $=$
$7+4+3+1+1+3+4$ $=23 \mathrm{~cm}$

$$
\begin{aligned}
23 \times 250 & =5750 \mathrm{~cm} \\
& =57.5 \mathrm{~m}
\end{aligned}
$$

Gate: 1 cm wide
$1 \times 250=250 \mathrm{~cm}$

$$
=2.5 \mathrm{~m}
$$


$>$ draw scale plans from given dimensions (plans should be labelled with scale used)
eg The following diagram shows a sketch of a country park visitor centre and its surroundings.

## Not to scale



Draw a scale plan of the visitor centre.
19. Use coordinates in 2-D, positive and negative, to specify the positions of points
> identify coordinates - read horizontal axis (x) before vertical axis (y)
eg identify the coordinates of the points marked

eg find coordinate that makes right angle triangle


$$
\begin{aligned}
& x \quad 5,3 \\
& \text { or }-5,-4 \\
& \quad \text { Answer }
\end{aligned}
$$

identify map coordinates (references)
eg The map below shows four campsites A, B, C, D. Some campers decide to stay overnight at the campsite grid reference 115240. The next day they move to campsite grid reference 128255.

Draw a line to show the route they take. (Answer shown as arrow)

$X=$ campsite
identify alpha numeric coordinates
eg A pilot flies from a point A2 (Cornwall) to London and then to point C7 (Liverpool) Draw his route on the map.
In which direction must he fly from A2 to London? (North west)

- From London to C7 (North east)



## 20. Understand and use common 2-D representations of 3-D objects

> Understand drawings and plans
eg The drawing shows a bedroom
What is the area of the wall behind the bed? $2.5 \times 2.5=6.25 \mathrm{~m}^{2}$
What is the area of the floor?
$2.5 \times 3.5=8.75 \mathrm{~m}^{2}$
What is the volume of the room?
$2.5 \times 2.5 \times 3.5=\mathbf{2 1 . 8 7 5} \mathbf{m}^{\mathbf{3}}$

eg What is the approximate volume of this drinks can?

$$
\begin{aligned}
V & =\pi r^{2} h \\
V & =\pi \times 3.25^{2} \times 11 \\
& =365 \mathrm{~cm}^{3}
\end{aligned}
$$



## 21. Draw 3-D shapes to include plans and elevations

recognise given plans and elevations
eg Which one of the sketches shows the elevation of the left side of the building? (Answer C)


A

B

C

D
Candidates should understand that co-ordinates can be presented, or written in horizontal and vertical formats
eg The diagram shows a cross section of a metal bar.

angles (p35ff) in this context.

Which one of the following is the side elevation? (Answer C)

A

B

C

D

Candidates should be able to apply underpinning knowledge about the properties of shapes (see p24f) and
$\mathrm{Eg}:(-2,1)$ is the same as $(-2,1)$
> draw top view plans from drawings and sketches eg the drawing shows one of the Great Pyramids
.Draw a top plan view of the Pyramid

## Great Pyramid


> draw elevations from drawings and sketches
eg the drawing shows a greenhouse
Draw a side elevation of the greenhouse

22. Calculate values of angles and/or coordinates with 2-D and 3-D shapes
$>$ calculate with reference to standard angles: right angle $90^{\circ}$; straight line $180^{\circ}$; point $360^{\circ}$

eg straight line $180^{\circ}$
$a+35=180$
$a=145^{\circ}$

eg angles round a point $360^{\circ}$
$a+50+130+50=360$
$a=130^{\circ}$
eg opposite angles are eaual

eg angles round a point $360^{\circ}$ eg application in pie chart $a+b+c=360^{\circ}$
> calculate with reference to interior angles of standard 2-D shapes: triangle $180^{\circ}$; quadrilateral $(4$ sides -2$) \times 180=360^{\circ}$; pentagon ( 5 sides -2$) \times 180=540^{\circ}$;
hexagon $(6$ sides -2$) \times 180=720^{\circ}$

eg angles in triangle add up to $180^{\circ}$
$a+57+90=180$
$a=33^{\circ}$

> eg angles in quadrilateral add up to $360^{\circ}$
> $a+150+55+70=360$
> $a=85^{\circ}$
eg angles in regular hexagon add up to (6-2) $\times 180=720^{\circ}$ $a=720 \div 6=120^{\circ}$
> calculate angles with reference to parallel lines


```
a+b+c+d=360
(angles in quadrilateral)
c+f = 180}\mp@subsup{}{}{\circ}\mathrm{ (straight line)
c+d = 180}\mp@subsup{}{}{\circ}\mathrm{ and
a+b=180}\mp@subsup{}{}{\circ}\mathrm{ and
a+d=180
b+c=180}\mp@subsup{}{}{\circ}\mathrm{ (interior angles)
e=d (opposite angles)
e=f(corresponding angles)
```


> calculate angles using combinations of above
eg calculate angles $a, b, c$

$a=110^{\circ}$
$b=60^{\circ}$
$c=120^{\circ}$
check $110+60+120+70=360$
eg the diagram shows a regular polygon calculate angle a


$$
a=54^{\circ}
$$

## 23. Calculate the median and mode of a set of quantities

> calculate median (odd number of data)
eg the table shows the price of petrol in petrol stations in a town

| Petrol prices per litre (p) |  |  |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 118.9 | 121.9 | 119.9 | 116.9 | 129.9 | 117.9 | 119.9 | 115.9 | 116.9 |

Work out the median price for one litre of petrol:
115.9116 .9116 .9117 .9118 .9119 .9119 .9121 .9129 .9

## Answer 118.9p

> calculate median (even number of data) eg the table shows the annual pay of a company's workers

| Workers annual pay (£) |
| :---: |
| 23500 |
| 18900 |
| 28900 |
| 24750 |
| 19300 |
| 39780 |
| 19250 |
| 22590 |

Work out the median pay for the company.
1890019250193002259023500247502890039780
median $=\frac{22590+23500}{2}=23045$

## Answer £23045

> calculate mode
eg a company sends letters by post.
The table shows the weights of the letters sent this week.

| Weight of letters in grams(g) |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- |
| 24.4 | 25.5 | 25.0 | 25.3 | 24.4 |
| 26.5 | 25.5 | 24.9 | 24.4 | 25.5 |
| 25.5 | 25.1 | 25.5 | 24.2 | 24.5 |

What is the modal value for the weight of the letters?

| Weight | Tally | Weight | Tally |
| :--- | :--- | :--- | :--- |
| 24.4 | III | 26.5 | I |
| $\mathbf{2 5 . 5}$ | IIII | 24.9 | I |
| 25 | I | 25.1 | I |
| 25.3 | I | 24.2 | I |
|  |  | 24.5 | I |

Answer 25.5g

## 24. Estimate the mean of a grouped frequency distribution from discrete data

$>$ find mean from grouped data in a chart
eg find the mean number of goals scored in each match


| Goals scored (x) |  | Frequency (f) (ie number of times ) | Answer <br> Calculate fx 's and n then mean $=\Sigma \mathrm{fx} / \mathrm{n}$ |  |
| :---: | :---: | :---: | :---: | :---: |
| 0 | x | 3 | = 0 | $\begin{gathered} \text { mean }= \\ 51 \div 25=\mathbf{2 . 0 4} \\ \text { (goals per match) } \end{gathered}$ |
| 1 | X | 5 | = 4 |  |
| 2 | X | 9 | =18 |  |
| 3 | X | 5 | = 15 |  |
| 4 | X | 2 | =8 |  |
| 5 | X | 1 | =5 |  |
| 6 or more | x | 0 | =0 |  |
|  |  | 25 | 51 |  |

$>$ find mean from grouped data in a table
$>$ understand format eg $63<\mathrm{g} \leq 65$ may be interpreted as ( a weight in) g is between 63 g and 65 g in order to determine a mid point $\frac{63+65}{2}=64 \mathrm{~g}$
eg estmate the mean weight of these large eggs

| Weights of large eggs |  | Answer <br> Calculate midpoints, then fx's and n then mean $=$ $\sum \mathrm{fx} / \mathrm{n}$ |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Weight in grams | Number of eggs |  |  |  |  |
| $63<\mathrm{g} \leq 65$ | 22 | x | 64 | =1408 | $\begin{gathered} \text { mean }= \\ 6728 \div 100=\mathbf{6 7 . 2 8 g} \end{gathered}$ |
| $65<\mathrm{g} \leq 67$ | 27 | X | 66 | =1782 |  |
| $67<\mathrm{g} \leq 69$ | 26 | x | 68 | = 1768 |  |
| $69<\mathrm{g} \leq 71$ | 15 | x | 70 | =1050 |  |
| $71<\mathrm{g} \leq 73$ | 10 | x | 72 | = 720 |  |
|  | 100 |  |  | 6728 |  |

## 25. Use mean, median, mode and range to compare 2 sets of data.

> calculate averages: mean, median, mode
$>$ choose the most suitable average to use and explain choice eg when comparing a given result, use the same average as the given result understand eg median is considered better average to use (than mean) if data is skewed or there are outliers
eg mean is the average of choice when data is evenly distributed (not skewed, no outliers) because it takes account of all the data
eg mode is best reserved for category (non-continuous data) and should not be used with very small data sets
> calculate range and understand that range is a measure of the consistency or variation of data
> explain comparisons using figures
eg An events organiser knows that the site she used last year (Site A) has average (mean) sunshine in June of 215 hours with a range of 99 hours.
She considers two other sites (Site B and Site C) and finds the following information.

| Total hours of sunshine in June |  |  |
| :--- | :--- | :--- |
|  | Sunshine (hours) |  |
| Year | Site B | Site C |
| 2008 | 213.70 | 192.70 |
| 2009 | 224.20 | 193.60 |
| 2010 | 265.00 | 198.80 |
| 2011 | 187.70 | 182.90 |
| 2012 | 282.70 | 244.50 |
| 2013 | 151.60 | 136.50 |
| 2014 | 158.40 | 141.70 |
| 2015 | 239.10 | 188.50 |
| 2016 | 169.50 | 151.90 |
| 2017 | 248.00 | 164.50 |
| 2018 | 194.650 | 197.30 |
| 2019 | 245.50 | 215.10 |

She wants a site with the best chance of sunshine.
Which Site would be best for her? Explain your answer.
Site A given mean = 215 hours and range 99 hours.
Need to compare means and range.
Site B mean $=2580.00 \div 12=215$ range $=282.7-151.6=131.1$
Site C mean $=2208.00 \div 12=184$ range $=244.5-136.5=108$
She should stay with Site $B$ because site $C$ has lower mean sunshine. Sites $A$ and $B$ have the same average sunshine but Site $A$ has lower range which is more consistent.
(Candidates are not expected to give such a detailed explanation, but could explain in terms of eg 215 hours is same for $A$ and $B, 184$ (C) is less AND A has lower range than $B$, so less variation)
eg A team manager has three players selected for the next match.

| Player | Average score (median) <br> over last eight matches | Range of scores <br> over last eight matches |
| :--- | :--- | :--- |
| Archie | 105 | 26 |
| Baz | 101 | 37 |
| Cathy | 99 | 32 |

She needs one more player to make up the team.
She looks at the scores of two more players.

| Scores in last eight matches |  |
| :--- | :--- |
| Dave | Elaine |
| 78 | 87 |
| 48 | 98 |
| 102 | 101 |
| 98 | 84 |
| 84 | 93 |
| 101 | 79 |
| 67 | 87 |
| 96 | 97 |

She wants the best and most consistent scorer.
Which player should the team manager select? Explain your answer.
Find median as the other players' averages are medians
Dave median: $486778849698101102 \quad \frac{84+96}{2}=90$

$$
\text { range }=102-48=54
$$

Elaine median 79848787939798101

$$
\frac{87+93}{2}=90
$$

range $=101-79=\mathbf{2 2}$
I would choose Elaine because the averages are equal 90 but Elaine's range 22 is lower than Dave's 54. Elaine has more consistency.

## 26. Work out the probability of combined events including the use of diagrams and tables including two-way tables

> work out the probability of combined events using a table eg what is the probability that two consecutive of this spinner will score more than 10 ? Give your answer as a fraction.


Note firstly 6 and 7 are missing
So the only way of getting more than ten is if 8 is one of the throws
There are 36 possibilities ( $6 \times 6$ ) for spinning twice, only when 8 and a 3 or more are spun will the total be more than 10, ie there are 7 possibilities:


Answer $\frac{7}{36}$
$>$ work out the probability of combined events using a diagram
eg A commuter travels every day by train from Leeds to Halifax in the morning and returns in the evening,
The train company publishes data for train time arrivals.

|  | On time (\%) |  |
| :--- | :--- | :--- |
|  | Morning | Evening |
| Leeds to Halifax | $80 \%$ | $75 \%$ |
| Halifax to Leeds | $90 \%$ | $60 \%$ |

What is the probability that, on one day, the commuter's train will be late both in the morning and in the evening? Give your answer as a decimal. Show your working as a tree diagram.


## 27. Express probabilities as fractions, decimals and percentages

> calculate probabilities of events as fractions
Spinning wheel game

eg If the wheel is spun again what is the chance of being the winner? Give your answer as a fraction in its simplest form.
of 24 sections; 3 are s

$$
\frac{3}{24}=\frac{1}{8} \quad \text { Answer }
$$

eg What is the probability of spinning a and a consecutive spins. Give your answer as a fraction in its simplest form.

$$
\begin{aligned}
& =\frac{6}{24}=\frac{1}{4} \quad=\frac{1}{8} \\
& \frac{1}{4} x \frac{1}{8}=\frac{1}{32} \quad \text { Answer }
\end{aligned}
$$

> calculate probabilities of events as percentages
$>$ eg A pack of cards contains 52 cards including four aces


A player takes two cards at random from the pack. They are both aces.


The player takes another card from the pack at random.
What is the percentage probability that this card will also be an ace? Show your answer in the diagram

There are 50 cards left, two of them will be the remaining aces.
Probability $=\frac{2}{50}=\frac{4}{100}=4 \%$


0\%
50\%
100\%
eg Members of a studio audience are asked to rate a new programme on a 3 point scale: like, dislike, not sure. The results are shown in the table below.

| age | like | dislike | not sure |
| :--- | :--- | :--- | :--- |
| under 20 | 10 | 30 | 0 |
| $20-30$ | 25 | 8 | 7 |
| over 30 | 26 | 5 | 9 |

A researcher picks a member of the audience at random.
What is the probability that the audience member will be under 20 and dislike the programme?
Give your answer as a decimal
Total number of audience members $=120$
Under 20 dislikes = 30
Probability $=30 \div 120=\mathbf{0 . 2 5}$ Answer

## 28. Draw and interpret scatter diagrams and recognise positive and negative correlation

Note: candidates should also be familiar with all other graphical presentations specified at lower levels eg bar charts, pie charts, tally charts, line graphs
> draw and label scatter diagrams (scatter graphs)
$>$ recognise and explain negative correlation le $y$ axis decreases as $x$ axis increases .
eg The Aquarium is an indoor attraction at a seaside town. The table shows the number of visitors at weekends during July and August and the hours of sunshine recorded

Visitors to the Aquarium - weekends July and August

| hours of sunshine | 12 | 0 | 16 | 6 | 16 | 20 | 14 | 10 | 6 |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| number of visitors | 150 | 250 | 50 | 200 | 100 | 25 | 100 | 125 | 175 |

Draw a suitable graph to compare the number of visitors to The Aquarium compared to the hours of sunshine. Explain what your graph shows.


Candidates are expected to draw a trend line (line of best fit) to complete the scatter graph without being instructed to do so. It should be drawn so that there are approximately the same number of plots either side of the trend line.
The explanation (of negative correlation) should include a reference to the number of visitors ( y axis) decreasing as the hours of sunshine ( x axis) increase.
> add trend line to and analyse scatter diagrams
$>$ recognise and understand positive correlation y axis increases as x axis increases
eg The graph shows data about typing speeds and the average number of typing errors made in tests for job applicants.

Relationship between typing speed and accuracy


Add a trend line to the graph. Explain what the trend line shows.
Trend line added shown in red - candidates are expected to draw a straight line through points, so that there are approximately the same number of plots either side of the trendline The explanation (of positive correlation) should include a reference to the number of mistakes increasing ( y axis) as the typing speed increases.(x axis).

An office employs a typist who makes an average 1.5 mistakes at a typing speed of 60 words per minute. Add this plot to the graph. Is the typist better, worse or about the same as the average? Explain your answer.
The plot is shown in red. The explanation should recognise that the typist is better than average and should include reference to the plot being below the trend line, which means the typist makes fewer mistakes at 60 wpm than average (see also p 11 point 8.3).

| Total 60 marks <br> Time 1 hour 45 minutes (Section 1-25 minutes, Section 2-1 hour 20 minutes) |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | Total marks | $\begin{gathered} \hline \text { Calculator } \\ (75 \%) \end{gathered}$ | $\begin{gathered} \text { Non-calculator } \\ (25 \%) \end{gathered}$ | Underpinning skills (25\%) | Problem solving ( $75 \%$ ) |
| Section 1 <br> Non-calculator | 15 | 0 | 15 | 10 | 5 |
| Section 2 Calculator | 45 | 45 | 0 | 5 | 40 |
| Totals | 60 | 45 | 15 | 15 | 45 |
| Level 2 Subject Content Coverage <br> 23-25 of the 28 numbered content statements must be covered in each assessment version (ie 82-89\%) (need at least 75\% of numbered SCS from each content area) $100 \%$ of numbered statements must be covered over every three assessment versions |  |  |  |  |  |
| Must meet $100 \%$ of the problem-solving bullet points across the test All problem solving questions should contain attributes $A$ and $C$. <br> * A Task has little or no scaffolding; there is little guidance given to the student beyond a start point and a finish point. Question does not explicitly state the mathematical process(es) required for the solution ${ }^{* *} \mathrm{C}$ Information not given in mathematical form or in mathematical language; or there is a need for resuls to be interpreted or methods evaluated, eg in a real world context. <br> (p19 DfESubject Content Functional Skills Mathematics) |  |  |  |  |  |

## Appendix 3 Specifications for lower levels (subsumed in Level 2)

## Note: numbers refer to subject content specifications (SCS) in DfE Subject Content

## Using numbers and the number system



| 8. Divide two-digit whole numbers by single-digit whole numbers and express remainders | 3. Divide three-digit whole numbers by single and double digit whole numbers and express remainders | 3. Multiply and divide whole numbers and decimals by $10,100,1000$ |
| :---: | :---: | :---: |
| 9. Approximate by rounding to the nearest 10 , and use this rounded answer to check results | 5. Approximate by rounding numbers less than 1000 to the nearest 10 or 100 and use this rounded answer to check results | 12. Approximate by rounding to a whole number or to one or two decimal places |
| 10. Recognise simple fractions (halves, quarters and tenths) of whole numbers and shapes | 7. Read, write and understand thirds, quarters, fifths and tenths including equivalent forms | 8. Read, write, order and compare common fractions and mixed numbers |
|  |  | 9. Find fractions of whole number quantities or measurements |
| 11. Read, write and use decimals to one decimal place | 8. Read, write and use decimals up to two decimal places | 10. Read, write, order and compare decimals up to three decimal places |
|  | 9. Recognise and continue sequences that involve decimals | 11. Add, subtract, multiply and divide decimals up to two decimal places |
|  |  | 13. Read, write, order and compare percentages in whole numbers |
|  |  | 14. Calculate percentages of quantities, including simple percentage increases and decreases by $5 \%$ and multiples thereof |
|  |  | 15. Estimate answers to calculations using fractions and decimals |

16. Recognise and calculate equivalences between common fractions, percentages and decimals
17. Work with simple ratio and direct proportions
18. Use simple formulae expressed in words for one or two-step operations
19. Follow the order of precedence of operators

| Using common measures, shape and space |  |  |  |
| :---: | :---: | :---: | :---: |
| 5. Recognise coins and notes and write them in numbers with the correct symbols ( $£ \& p$ ), where these involve numbers up to 20 | 12. Calculate money with pence up to one pound and in whole pounds of multiple items and write with the correct symbols ( $£$ or p) | 10. Calculate with money using decimal notation and express money correctly in writing in pounds and pence | 18. Calculate simple interest in multiples of $5 \%$ on amounts of money |
|  |  |  | 19. Calculate discounts in multiples of $5 \%$ on amounts of money |
|  |  | 11. Round amounts of money to the nearest $£ 1$ or 10p |  |
| 6. Read 12 hour digital and analogue clocks in hours | 13. Read and record time in common date formats, and read time displayed on analogue clocks in hours, half hours and quarter hours, and understand hours from a 24-hour digital clock | 12. Read, measure and record time using am and pm |  |
| 7. Know the number of days in a week, months, and seasons in a year. Be able to name and sequence | 7. Know the number of hours in a day and weeks in a year. | 13. Read time from analogue and 24hour digital clocks in hours and minutes |  |
| 8. Describe and make comparisons in words between measures of items including size, | 14. Use metric measures of length including millimetres, centimetres, metres and kilometres | 15. Compare metric measures of length including millimetres, centimetres, metres and kilometres | 22. Calculate the area and perimeter of simple shapes including those that are made up of a combination of rectangles |


| length, width, height, weight and capacity |  |  |  |
| :---: | :---: | :---: | :---: |
|  | 15. Use measures of weight including grams and kilograms | 14. Use and compare measures of length, capacity, weight and temperature using metric or imperial units to the nearest labelled or unlabelled division | 23. Calculate the volumes of cubes and cuboids |
|  |  | 16. Compare measures of weight including grams and kilograms | 20. Convert between units of length, weight, capacity, money and time, in the same system |
|  | 16. Use measures of capacity including millilitres and litres | 17. Compare measures of capacity including millilitres and litres |  |
|  | 17. Read and compare positive temperatures |  |  |
|  | 18. Read and use simple scales to the nearest labelled division | 18. Use a suitable instrument to measure mass and length | 21. Recognise and make use of simple scales on maps and drawings |
| 9. Identify and recognise common 2-D and 3-D shapes including circle, cube, rectangle (including square) and | 19. Recognise and name 2-D and $3-\mathrm{D}$ shapes including pentagons, hexagons, cylinders, cuboids, pyramids and spheres | 19. Sort 2-D and 3-D shapes using properties including lines of symmetry, length, right angles, angles including in rectangles and triangles | 24. Draw 2-D shapes and demonstrate an understanding of line symmetry and knowledge of the relative size of angles |



| 13. Read and draw simple <br> charts and diagrams <br> including a tally chart, <br> block diagram/graph | 25. Take information from <br> one format and represent <br> the information in <br> another format including <br> use of bar charts | 23. Organise and represent information <br> in appropriate ways including tables, <br> diagrams, simple line graphs and bar <br> charts | 27. Represent discrete data in tables, diagrams <br> and charts including pie charts, bar charts <br> and line graphs |
| :--- | :--- | :--- | :--- |
|  |  |  | 28. Group discrete data and represent grouped <br> data graphically |
|  |  | 29. Find the mean and range of a set of <br> quantities |  |

## Solving mathematical problems and decision making

| Entry Level 1 <br> use the knowledge and skills listed above to recognise a simple mathematical problem and obtain a solution. A simple mathematical problem is one which requires working through one step or process and which draws upon knowledge and/or skills from one mathematical content area | Entry Level 2 <br> use the knowledge and skills listed above to recognise a simple problem and obtain a solution. <br> A simple problem is one which requires working through one step or process and which draws upon knowledge and/or skills from one mathematical content area | Entry Level 3 <br> use the knowledge and skills listed above to recognise a simple problem and obtain a solution. <br> A simple problem is one which requires working through one step or process. and which draws upon knowledge and/or skills from one mathematical content area | Level 1 <br> use the knowledge and skills listed above to recognise and obtain a solution or solutions to a straightforward problem. <br> A straightforward problem is one that requires students to either work through one step or process or to work through more than one connected step or process and some of which draw upon a combination of any two of the mathematical content areas and require students to make connections between those content areas |
| :---: | :---: | :---: | :---: |
| - Use given mathematical information and recognise and use simple mathematical terms appropriate to Entry Level 1 | Use given mathematical information including numbers, symbols, simple diagrams and charts | - Use given mathematical information including numbers, symbols, simple diagrams and charts |  |
|  | Recognise, understand and use simple mathematical terms appropriate to Entry Level 2 | - Recognise, understand and use simple mathematical terms appropriate to Entry Level 3 | - Read, understand and use mathematical information and mathematical terms used at this level |
|  |  |  | Address individual problems as described above |


| - Use the methods given above to produce, check and present results that make sense | Use the methods given above to produce, check and present results that make sense | - Use the methods given above to produce, check and present results that make sense to an appropriate level of accuracy | Use knowledge and understanding to a required level of accuracy |
| :---: | :---: | :---: | :---: |
|  |  |  | Analyse and interpret answers in the context of the original problem |
|  |  |  | Check the sense, and reasonableness, of answers |
| - Provide a simple explanation for those results | Present appropriate explanations using numbers, measures, simple diagrams, simple charts and symbols appropriate to Entry Level 2 | - Present results with appropriate and reasoned explanation using numbers, measures, simple diagrams, charts and symbols appropriate to Entry Level 3. | Present results with appropriate explanation and interpretation demonstrating simple reasoning to support the process and show consistency with the evidence presented |
| The context for simple problems at this level should be familiar to all students and easily described. | The context for simple problems at this level should be familiar to all students and easily described. | The context for simple problems at this level should be familiar to all students. | The context of individual problems at this level will require some comprehension in order for the student to be able independently to identify and carry out an appropriate mathematical approach. |

## Contact us

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## About City \& Guilds

Since 1878 we have worked with people, organisations and economies to help them identify and develop the skills they need to thrive. We understand the life changing link between skills development, social mobility, prosperity and success. Everything we do is focused on developing and delivering high-quality training, qualifications, assessments and credentials that lead to jobs and meet the changing needs of industry.

We work with governments, organisations and industry stakeholders to help shape future skills needs across industries. We are known for setting industry-wide standards for technical, behavioural and commercial skills to improve performance and productivity. We train teams, assure learning, assess cohorts and certify with digital credentials. Our solutions help to build skilled and compliant workforces.

[^1]
[^0]:    DfE Subject Content: Overview of sections (Level 2)

    ## Use of numbers and the number system

    Students at Level 2 are expected to be able to use numbers of any size; read, write and make use of positive and negative integers of any size; use, order and compare integers, fractions, decimals, percentages and ratios as well as recognise the value of a digit in any whole or decimal number. They can use numerical and spatial patterns for a purpose and calculate with, and convert between, numbers written as fractions, decimals, percentages and ratios.
    Use of measures, shape and space
    Students at Level 2 are expected to be able to handle relationships between measurements of various kinds, use angles and coordinates when involving position and direction and make use of geometric properties in calculations with 2$D$ and 3-D shapes and understand the relationships between them.

    ## Handle information and data:

    Students at Level 2 are expected to be able to construct, interpret and evaluate a range of statistical diagrams. They can

    ## Solving mathematical problems and decision making

    Students at Level 2 are expected to be able to use knowledge and skills to recognise and obtain a solution or solutions to a complex problem. A complex problem is one which requires a multistep process, typically requiring planning and working through at least two connected steps or processes. Individual problems are based on a combination of the knowledge and/or skills from the mathematical content areas (number and the number system; measures, shape and space; information and data). At Level 2 it is expected that the student will be able to address individual problems some of which draw upon a combination of all three mathematical areas and require students to make connections between those content areas.
    The context of individual problems at this level will require interpretation and analysis in order for the student to be able independently to identify and carry out an appropriate mathematical process or processes.

[^1]:    Every effort has been made to ensure that the information contained in this publication is true and correct at time of going to press. However, City \& Guilds' products and services are subject to continuous development and
    improvement and the right is reserved to change products and services from time to time. City \& Guilds cannot accept responsibility for any loss or damage arising from the use of information in this publication.

